## Eigenvalues and Eigenfunctions

Math 330
Consider the ODE:

$$
\frac{d^{2} v}{d x^{2}}=\lambda v
$$

1. What is the solution to the ODE...
(a) $\ldots$ if $\lambda>0$ ?
(b) $\ldots$ if $\lambda=0$ ?
(c) $\ldots$ if $\lambda<0$ ?
2. Which of the solutions you found in \#1 satisfy the boundary conditions $v^{\prime}(0)=0$ and $v^{\prime}(\pi)=0$ ?
3. Which of the solutions you found in \#1 satisfy the periodic boundary conditions $v(-\pi)=v(\pi)$ and $v^{\prime}(-\pi)=v^{\prime}(\pi)$ ?
