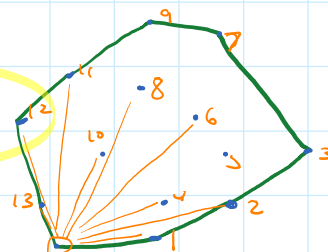


gift wrapping:  $O(nh)$

## GRAHAM SCAN ALGORITHM: $O(n \log n)$

1. Choose the lowest point as the anchor —  $O(n)$
2. Sort all other points by their angle with the anchor  $O(n \log n)$
3. Construct the hull following this ordering:
  - Append next point to the hull
  - Remove any reflex angles ("right turns") that result

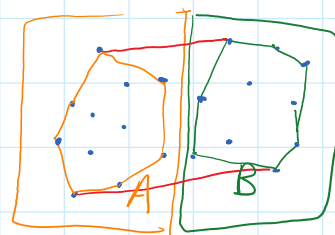


## DIVIDE AND CONQUER ALGORITHM — $O(n \log n)$

1. Sort points by x-coord. —  $O(n \log n)$
2. Divide the points:
  - A = left half of the points
  - B = right half

$O(\log_2 n)$  divisions

3. Find convex hulls of A and B recursively — call divide and conquer on A and B  
 If A or B contains  $\leq 3$  points, then stop dividing; return these points.

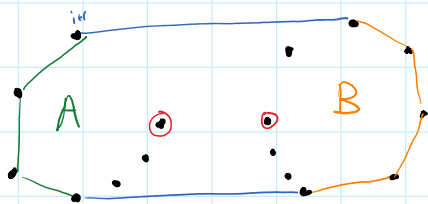


- $O(n)$
4. Merge hulls of A and B  
 most tricky part
- $O(n \log n)$

$$\log_x^n = \frac{1}{\log_x A} \log_x^n$$

$$O(\log_x n) = O(\log_x n)$$

Merging two hulls in  $O(n)$  time:



Identify rightmost vertex of A,  
and leftmost vertex of B.