## Special Triangulations

Math 282 Computational Geometry

1. Justify the following: Let $a, b, c, d$ be points in the plane, with a triangulation consisting of triangles $\Delta a b c$ and $\Delta a c d$. Then edge $\overline{a c}$ is a legal edge of the Delaunay triangulation if and only if $d$ is outside of the circumcircle of $\Delta a b c$.
2. Justify the following: Let $a$ and $b$ be points in a planar point set $S$. If there exists a circle passing through $a$ and $b$ that contains no other points of $S$ in its interior, then edge $\overline{a b}$ is an edge of the Delaunay triangulation of $S$.
3. Suppose you have a Delaunay triangulation of a set of points $S$. If you add a new point $p$, describe an algorithm for updating the triangulation to obtain the Delaunay triangulation of $S \cup\{p\}$.
