

DEMONSTRATIONS:

X:

x	1	2	3	4
$p(x)$	0.4	0.3	0.2	0.1

R: histogram of simulated values
 ↪

```

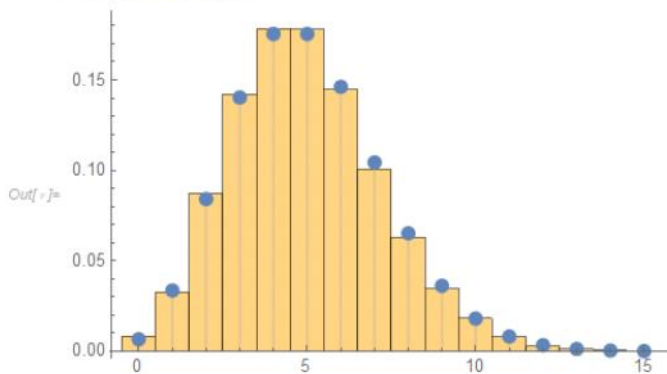
1 randvar <- function(){
2   u <- runif(1)
3   if(u < 0.4){
4     x <- 1
5   } else if(u < 0.7){
6     x <- 2
7   } else if(u < 0.9){
8     x <- 3
9   } else {
10    x <- 4
11  }
12  return(x)
13 }
14
15 randvar()
16
17 vals <- replicate(1000, randvar())
18
19 vals
20 hist(vals)
    
```

Mathematica: simulation of Poisson-distributed values:

```

randVal := Module[{u, x},
  u = RandomReal[];
  x = Which[u < 0.4, 1, u < 0.7, 2, u < 0.9, 3, True, 4];
  Return[x]
]

In[ ]:= vals = RandomVariate[PoissonDistribution[5], 10000];
In[ ]:= hist = Histogram[vals, Automatic, "Probability"]
In[ ]:= disc = DiscretePlot[Exp[-5] 5^x / x!, {x, 0, 15}, PlotMarkers -> {Automatic, Medium}]
In[ ]:= Show[hist, disc]
    
```



QUEUE SIMULATIONS:

```
R: # queue simulation as a function, with max size 100, stops when queue is empty
queueSimulation <- function(){
  queueSize = 1
  time = 1
  while(queueSize > 0){
    time = time + 1
    x = rpois(1, 5)
    if(queueSize + x > 100){
      queueSize = 100
    } else {
      queueSize = queueSize + x
    }
    y = rpois(1, 5)
    if(y > queueSize){
      queueSize = 0
    } else {
      queueSize = queueSize - y
    }
  }
  return(time)
}

# estimate time at which queue is empty
times = replicate(100000, queueSimulation())
times
mean(times)
sd(times)
```

Mathematica:

```
In[1]:= queueSim[] := Module[{},
  queueSize = 1;
  time = 0;
  While[queueSize > 0,
    time += 1;
    x = RandomVariate[PoissonDistribution[5]];
    queueSize = queueSize + x;
    If[queueSize > 100, queueSize = 100];
    y = RandomVariate[PoissonDistribution[5]];
    If[y > queueSize, queueSize = 0, queueSize = queueSize - y];
    (*Print["at time ",time," the queue contains: ",queueSize]*)
  ];
  (*Print["time until the queue is empty: ",time];*)
  Return[time]
]
```

```
In[2]:= queueSim[]
```

```
Out[2]= 17
```

```
In[3]:= vals = Table[queueSim[], 10000]
```

```
In[4]:= Mean[vals] // N
```

```
Out[4]= 52.3655
```

```
In[5]:= StandardDeviation[vals] // N
```

```
Out[5]= 245.383
```