

**PROBLEM:** Find 10 non-negative integers that sum to 100 and whose product is as big as possible.

Example: 5, 7, 20, 8, 10, 1, 19, 4, 6, 20

How many sets of 10 numbers are there that sum to 100? 6,292,069

States: set of 10 non-neg. integers that sum to 100:  $(n_0, n_1, \dots, n_9)$

Function: maximize  $f(n_0, n_1, \dots, n_9) = n_0 n_1 \dots n_9$   
 minimize  $g(n_0, n_1, \dots, n_9) = -n_0 n_1 \dots n_9$

Frequency distribution: minimum  $f(x)$  corresponds to max.  $e^{-f(x)/\sigma^2}$   
 ↑  
 frequency

frequency:  $e^{-g(n_0, n_1, \dots, n_9)/\sigma^2} = e^{n_0 n_1 \dots n_9 / \sigma^2}$   
 Too big!

IDEA: Maximize the log of the product:  $\log(n_0 n_1 \dots n_9 + 0.1)$   
 ↑  
 avoid  $\log(0)$

$$h(n_0, n_1, \dots, n_9) = \log(n_0 n_1 \dots n_9 + 0.1)$$

FREQUENCY:  $e^{-h/\sigma^2} = e^{-\log(n_0 n_1 \dots n_9 + 0.1)/\sigma^2}$

TRANSITIONS BETWEEN STATES:

EXAMPLE: 5, 7, 20, 8, 10, 1, 19, 4, 6, 20  
 ↓ ↓  
 5, 7, 20, 7, 10, 1, 19, 5, 6, 20