

# An Oscillator with a Parameter

Math 230

1. Find the solution to the initial value problem:

$$y'' + 10y = \cos(\omega t) \quad \text{with} \quad y(0) = 0, y'(0) = 0.$$

Here,  $\omega$  is a parameter. Make sure you consider all real values of  $\omega$ .

2. Plot your solution for the following values of  $\omega$ :

(a)  $\omega = 0$

(b)  $\omega = 2$

(c)  $\omega = 3$

(d)  $\omega = \sqrt{10}$

What do you observe? You may wish to plot solutions for other choices of  $\omega$ , or use the *Mathematica* `Manipulate` function to see the plot change as you adjust  $\omega$ .